tible to conformational changes, which is consistent with the expected effect of the cyclohexo groups on ring rigidity.

The $\log K$ values in Table III for the reactions of $\mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}$. and $\mathrm{Pb}^{2+}$ with II, IIIa, and IIIb are much larger than the corresponding values for the reactions of these metal ions with IV. ${ }^{17}$ In addition, the $\mathrm{Pb}^{2+}$ IV complex is reported to be less stable than the $\mathrm{Ba}^{2+}$-IV complex, which is the opposite trend to that seen in Table III for II, IIIa, and IIIb. The results of Shchori et al. ${ }^{17}$ with IV suggest that the effect of substitution of two benzo groups on II is to markedly lower complex stability for bivalent, but not univalent (Figure 1) metal ions and to reverse the $\mathrm{Pb}^{2+}, \mathrm{Ba}^{2+}$ stability order. On the other hand, the data in Figure 2 generally show trends opposite to these for IIIa and IIIb when compared with II.

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# Calorimetric Titration Study of the Interaction of Some Uni- and Bivalent Cations with Benzo-15-crown-5, 18-Crown-6, Dibenzo-24-crown-8, and Dibenzo-27-crown-9 in Methanol-Water Solvents, at $25^{\circ} \mathrm{C}$ and $\mu=0.1^{1}$ 

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#### Abstract

The interaction between $\mathrm{Na}^{+}, \mathrm{K}^{+}, \mathrm{Rb}^{+}, \mathrm{Cs}^{+}, \mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}$, and $\mathrm{Pb}^{2+}$ and the cyclic polyethers benzo-15-crown-5,18-crown-6, dibenzo-24-crown-8, and dibenzo-27-crown-9 in $\mathrm{CH}_{3} \mathrm{OH}-\mathrm{H}_{2} \mathrm{O}$ solvents has been studied using a calorimetric titration procedure. $\log \beta_{i}, \Delta H_{i}$, and $\Delta S_{i}$ values are calculated in those instances where sufficient amounts of heat were produced. Complexes having 1:1 metal-ligand stoichiometry resulted with these ligands except for the $\mathrm{Rb}^{+}$and $\mathrm{K}^{+}$-benzo- $15 \cdot$ crown. 5 systems at 70 and $80 w t \% \mathrm{CH}_{3} \mathrm{OH}$, which were found to be $1: 2$. As the cyclic polyether ring size increases, the $\Delta S$ values for the $1: 1$ reaction of a given cation become more negative, suggesting increased ligand conformational change upon complex formation.


Following the initial observation of Pedersen ${ }^{2}$ that certain cyclic polyethers selectively complex cations, extensive research has been conducted on the ability of compounds of this class to complex univalent and bivalent metal ions. ${ }^{3}$ A striking result
of this work was the observation that in aqueous solution certain of the cyclic polyethers (e.g., 18 -crown-6) show marked cation selective behavior, while others (e.g., 15 -crown- $5^{4}$ and dicyclohexo-24-crown-8 ${ }^{5}$ ) do not. Also, stoichiometry other
than $1: 1$ is observed ${ }^{2 b-d .3}$ under certain conditions. For example, when the cation is much larger than the ligand cavity, $1: 2$ cation to ligand complexes may be formed.

In the present investigation, the interactions of several uniand bivalent cations with ligands I-IV in solvents of several $\mathrm{H}_{2} \mathrm{O}-\mathrm{CH}_{3} \mathrm{OH}$ compositions have been studied by a calorimetric titration procedure. $\log \beta_{i}, \Delta H_{i}$, and $\Delta S_{i}$ values are calculated in those experiments where sufficient heat was produced. These thermodynamic values are used to evaluate the following factors as they affect complex stability and/or the formation of complexes with other than 1:1 stoichiometry: (1) the composition of the solvent; (2) the ratio of cation diameter to polyether ring cavity diameter; (3) the number of potential cation coordination sites in the ring; and (4) the flexibility of the ring. These and other factors which determine the magnitude of $\log \beta_{i}$ values for the formation of cationcyclic polyether complexes have been presented and discussed. ${ }^{6-9}$


I
benzo-15-crown-5


II
18-crown-6

dibenzo-24-crown-8

dibenzo-27.crown-9

## Experimental Section

Materials. The following chemicals were used in the study: NaCl , $\mathrm{CaCl}_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$, and $\mathrm{BaCl} 2 \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Baker and Adamson, ACS reagent); KCl (Matheson, Coleman, and Bell, ACS reagent), RbCl (Apache Chemicals, $99.9 \%$ ); CsCl (J. T. Baker Chemical Co., 99.9\%); $\mathrm{SrCl}_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Baker Analyzed reagent): $\mathrm{Co}\left(\mathrm{ClO}_{4}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$. $\mathrm{Cu}\left(\mathrm{ClO}_{4}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}, \mathrm{Pb}\left(\mathrm{ClO}_{4}\right)_{2} \cdot 3 \mathrm{H}_{2} \mathrm{O}$, and $\mathrm{Zn}\left(\mathrm{ClO}_{4}\right)_{2} \cdot \mathrm{H}_{2} \mathrm{O}$ (G. Frederick Smith Chemical Co., reagent); $\mathrm{Cd}\left(\mathrm{ClO}_{4}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Alfa Inorganics); $\mathrm{NH}_{4} \mathrm{Cl}$ (Fisher, reagent); methanol (Baker and Adamson Special Reagent Code 1217). Compound II (Peninsular Chemical Research, Inc., $99 \%$ ) was used without further purification, while the remaining cyclic polyethers (I, III, and IV) were synthesized in our laboratories from reagent grade chemicals using the following procedures.
Compound I was prepared from catechol and 1.11-dichloro-$3,6,9$-trioxaundecane ${ }^{2 b}$ using the procedure given by Pedersen; ${ }^{2 b} \mathrm{mp}$
$79-79.5^{\circ} \mathrm{C}$ (lit. $.^{26} 79-79.5^{\circ} \mathrm{C}$ ). Compound III was prepared from catechol and 1,2-bis(2-chloroethoxy)ethane (Eastman) with potassium hydroxide as base, following the procedure used by Pedersen; ${ }^{26}$ $\mathrm{mp}, 102-103{ }^{\circ} \mathrm{C} \cdot{ }^{10} \mathrm{NMR}\left(\mathrm{CDCl}_{3}\right) \delta 3.85(\mathrm{~s}, 8 \mathrm{H}), 3.91(\mathrm{~m}, 8 \mathrm{H}), 4.18$ $\left(\mathrm{m}, 8 \mathrm{H}\right.$ ), and 6.91 ( $\mathrm{s}, 8 \mathrm{H}$ ). Anal. Calcd for $\mathrm{C}_{24} \mathrm{H}_{32} \mathrm{O}_{8}: \mathrm{C}, 64.27 ; \mathrm{H}$, 7.19. Found: C, 64.17; H, 7.06.

The preparation of compound IV was accomplished using the following procedures. A mixture of $20 \mathrm{~g}(0.1 \mathrm{~mol})$ of catechol mono-2tetrahydropyranyl ether, ${ }^{11} 12 \mathrm{~g}$ of sodium hydroxide, and 50 ml of dimethyl sulfoxide was stirred under nitrogen at room temperature for I h. 1,11-Dichloro-3,6,9-trioxaundecane ${ }^{2 b}$ ( $35 \mathrm{~g}, 0.15 \mathrm{~mol}$ ) was slowly added and the mixture was stirred at room temperature for an additional 3 h . Water was added to dissolve the solid and the mixture was extracted with diethyl ether. The ether extract was condensed to $100 \mathrm{ml}, 50 \mathrm{ml}$ of 7 M HCl was added, and the mixture was stirred overnight. The aqueous layer was separated, washed with ether, and the combined ether layers were washed with a $10 \%$ aqueous NaOH solution. The NaOH extract was saturated with $\mathrm{CO}_{2}$ and continuously extracted with ether in a liquid-liquid extractor. The ether extract was dried over anhydrous $\mathrm{MgSO}_{4}$ to give 23.0 g ( $89 \%$ yield) of residue which gave a positive test for phenol and exhibited one large peak in the vapor-phase chromatograph. The residue was stirred with 10.3 g of NaOH in 50 ml of dimethyl sulfoxide for 30 min . $1,2-\operatorname{Bis}(2-$ chloroethoxy) ethane ( $25.5 \mathrm{~g}, 1.5$ equiv, 0.13 mol ) was added dropwise and the mixture was stirred for an additional 3 h . Water was added to dissolve the solid and the aqueous solution was extracted with ether to give a $4: 1$ mixture of 1,2 -bis( 2 -chloroethoxy)ethane and IV. The aqueous layer was further extracted with heptane continuously in a liquid-liquid extractor. The heptane extract, upon cooling, gave white crystals. Recrystallization from ether-hexane yielded 6.4 g of IV: mp $81.5-82.0^{\circ} \mathrm{C}$; NMR $\left(\mathrm{CDCl}_{3}\right) \delta 6.77(\mathrm{~s}, 12 \mathrm{H}), 3.96(\mathrm{~m}, 8 \mathrm{H}), 4.18$ (m, 8 H ), and 6.90 (s. 8 H ). Anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{36} \mathrm{O}_{9}: \mathrm{C}, 63.40 ; \mathrm{H}$. 7.37. Found: C, 63.48; H, 7.50.

Solution Preparation. The solvents were prepared from weighed amounts of methanol and boiled, doubly distilled water. Salt solutions ( $0.004-0.008 \mathrm{M}$ or $0.15-0.25 \mathrm{M}$ ) were prepared by dissolving the appropriate weight of each salt in the methanol-water solvents. The $\mathrm{NaCl}, \mathrm{KCl}, \mathrm{RbCl}$, and CsCl salts were dried at $120^{\circ} \mathrm{C}$ for 24 h prior to weighing. The $\mathrm{Pb}\left(\mathrm{ClO}_{4}\right)_{2}$ solution was standardized gravimetrically by precipitation of $\mathrm{PbCrO}_{4}$. The $\mathrm{SrCl}_{2}$ and $\mathrm{CaCl}_{2}$ solutions were standardized by Mohr titration. The $\mathrm{BaCl}_{2}$ solution was standardized volumetrically by observing the end point when a solution of barium "rhodizonate" was converted to barium sulfate.

The cyclic polyether solutions were prepared by dissolving known weights of I, II, III, and IV in the appropriate solvent to give final concentrations of 0.1 or 0.01 M .

Procedure and Calculations. The calorimetric determinations were made at $25^{\circ} \mathrm{C}$ using a Tronac precision titration calorimeter (Tronac, Inc., Orem, Utah). ${ }^{12-15}$ The cyclic polyether solutions were titrated into the metal ion solutions whenever possible. However. in the cases of 111 and IV, where the solubilities of the cyclic polyethers were not sufficient to give measurable results, the procedure was reversed and the metal ion solutions were titrated into the cyclic polyether solutions. Heat of dilution corrections were made by titrating solutions of the cyclic polyether or metal ion solutions into the solvent.
The method used to calculate $\log K$ and $\Delta H$ values from the calorimetric data using a nonlinear least-squares technique has been described. ${ }^{16}$ In most cases, the equation

$$
\begin{equation*}
\mathrm{M}^{n+}+\mathrm{L}=\mathrm{ML}^{n+} \quad \beta_{1}=K_{1}=\left[\mathrm{ML}^{n+}\right] /\left[\mathrm{M}^{n+}\right][\mathrm{L}] \tag{1}
\end{equation*}
$$

was found to adequately describe the reaction occurring in the calorimeter. However, for the reaction of $\mathrm{K}^{+}$with 1 in 60,70 , and $80 \%$ $\mathrm{CH}_{3} \mathrm{OH}$ and $\mathrm{Rb}^{+}$with I in $70 \% \mathrm{CH}_{3} \mathrm{OH}$, eq 1 did not adequately describe the experimental data. Use of eq 1 and

$$
\begin{equation*}
\mathrm{M}^{n+}+2 \mathrm{~L}=\mathrm{ML}_{2}{ }^{n+} \quad \beta_{2}=K_{1} K_{2}=\left[\mathrm{ML}_{2}{ }^{n+}\right] /\left[\mathrm{M}^{n+}\right][\mathrm{L}]^{2} \tag{2}
\end{equation*}
$$

gave results in all cases which could be satisfactorily fitted to the experimental heat values. However, there was not sufficient heat generated in the titration of $\mathrm{K}^{+}$with I in $60 \% \mathrm{CH}_{3} \mathrm{OH}$ (because of low solubility of I) to allow calculation of reliabie $\log \beta_{1}$ and $\log \beta_{2}$ values. Data coilected by the reverse titration of I with $K^{+}$, where the heat is not limited by solubility, are not sensitive to the presence of $1: 2$ species; hence, no $\log \beta$ values were calculated for the $\mathrm{K}^{+}-1$ system in $60 \% \mathrm{CH}_{3} \mathrm{OH}$. Log $\beta_{1}$ values for the $\mathrm{Na}^{+}-\mathrm{I}$ system at $70 \mathrm{wt} \%$ $\mathrm{CH}_{3} \mathrm{OH}$ calculated from heat data obtained using either $\mathrm{Na}^{+}$or 1 as

Table I. Log $\beta_{i}, \Delta H_{i}$, and $\Delta S_{i}$ Values for the Interaction of Cyclic Polyether Compounds with Several Univalent and Bivalent Metal lons at $25^{\circ} \mathrm{C}$ and $\mu=0.1^{a}$

| Ligand | $\mathrm{M}^{n+}$ | Solvent composition, wt $\% \mathrm{CH}_{3} \mathrm{OH}$ in $\mathrm{H}_{2} \mathrm{O}^{b}$ | $\log \beta_{i}$ | $i$ | $\begin{gathered} \Delta H_{i} \\ \mathrm{kcal} / \mathrm{mol} \end{gathered}$ | $\begin{gathered} \Delta S_{1}, \text { cal/ } \\ \text { (deg mol) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{Na}^{+}$ | 0 | $0.4{ }^{\text {c }}$ |  |  |  |
|  |  | 20 | $0.72 \pm 0.03$ | 1 | $-1.77 \pm 0.02$ | -2.6 |
|  |  | 40 | $1.17 \pm 0.12$ | 1 | $-2.63 \pm 0.11$ | -3.5 |
|  |  | 60 | $1.64 \pm 0.04$ | 1 | $-3.78 \pm 0.08$ | -5.2 |
|  |  | 70 | $1.99 \pm 0.10$ | I | $-3.82 \pm 0.07$ | -3.7 |
|  |  | 80 | $2.26 \pm 0.02$ | 1 | $-8.32 \pm 0.03$ | -17.6 |
|  | $\mathrm{K}^{+}$ | 0 | $0.38 \pm 0.10$ | 1 | $-2.33 \pm 0.10$ | -6.1 |
|  |  | 20 | $1.20 \pm 0.10$ | 1 | $-1.8 \pm 0.2$ | -0.5 |
|  |  | 40 | $1.92 \pm 0.04$ | 1 | $-2.51 \pm 0.03$ | 0.4 |
|  |  | 70 | $1.5 \pm 0.3$ | 1 | $d$ |  |
|  |  |  | $4.15 \pm 0.02$ | 2 | $-13.9 \pm 0.2$ | -27.6 |
|  |  | 80 | $2.2 \pm 0.2$ | 1 | $d$ |  |
|  |  |  | $4.80 \pm 0.05$ | 2 | $-15.50 \pm 0.13$ | -30.0 |
|  | $\mathrm{Rb}^{+}$ | 70 | $1.8 \pm 0.2$ | 1 | $d$ |  |
|  |  |  | $3.77 \pm 0.05$ | 2 | $-12.0 \pm 1.5$ | -23.5 |
|  | Cs ${ }^{+}$ | 70 | $1.70 \pm 0.01$ | 1 | $-2.43 \pm 0.05$ | -0.4 |
|  | $\mathrm{NH}_{4}{ }^{+}$ | 70 | $e$ |  |  |  |
|  | $\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}$ | 70 | $e$ |  |  |  |
|  | $\mathrm{Pb}^{2+}$ | 70 | $2.04 \pm 0.01$ | 1 | $-5.11 \pm 0.02$ | -7.8 |
|  | $\mathrm{Co}^{2+}, \mathrm{Cu}^{2+}, \mathrm{Zn}^{2+}, \mathrm{Cd}^{2+}$ | 70 | e |  |  |  |
| 11 | $\mathrm{Na}+$ | 70 | $2.76 \pm 0.02$ | 1 | $-4.89 \pm 0.01$ | -3.8 |
|  | $\mathrm{K}^{+}$ | 70 | $4.33 \pm 0.05$ | 1 | $-9.68 \pm 0.01$ | -12.7 |
|  | $\mathrm{Rb}^{+}$ | 70 | $3.46 \pm 0.10$ | 1 | $-9.27 \pm 0.05$ | -15.3 |
|  | $\mathrm{Cs}^{+}$ | 70 | $2.84 \pm 0.01$ | 1 | $-8.09 \pm 0.01$ | -14.1 |
|  | $\mathrm{Ca}^{2+}$ | 70 | $2.51 \pm 0.02$ | 1 | $-4.27 \pm 0.02$ | -2.8 |
|  | $\mathrm{Sr}^{2+}$ | 70 | $5.0 \pm 0.1$ | 1 | $-7.49 \pm 0.01$ | -2.5 |
|  | $\mathrm{Ba}^{2+}$ | 70 | $6.0{ }^{\prime}$ | 1 | $-10.66 \pm 0.01$ | -8.5 |
|  | $\mathrm{Pb}^{2+}$ | 70 | 6.51 | 1 | $-9.19 \pm 0.01$ | -1.1 |
| III | $\mathrm{Na}^{+}$ | 70 | $1.54 \pm 0.01$ | I | $-7.75 \pm 0.02$ | -18.9 |
|  | $\mathrm{K}^{+}$ | 70 | $2.42 \pm 0.01$ | 1 | $-8.54 \pm 0.01$ | -17.6 |
|  | $\mathrm{Rb}^{+}$ | 70 | $2.55 \pm 0.01$ | 1 | $-8.72 \pm 0.02$ | -17.6 |
|  | $\mathrm{Cs}^{+}$ | 70 | $2.48 \pm 0.01$ | 1 | $-8.93 \pm 0.02$ | -18.6 |
| iv | $\mathrm{Na}^{+}$ | 70 | $1.50 \pm 0.01$ | 1 | $-11.74 \pm 0.01$ | -32.5 |
|  | $\mathrm{K}^{+}$ | 70 | $2.86 \pm 0.01$ | 1 | $-9.50 \pm 0.01$ | -18.8 |
|  | $\mathrm{Cs}^{+}$ | 70 | $1.42 \pm 0.02$ | , | $-6.14 \pm 0.06$ | -14.1 |

[^0]titrant were the same within experimental uncertainty, indicating that only one species is present in this case.

## Results

The results of the study are given in Table I. $\log \beta_{i}, \Delta H_{i}$, and $\Delta S_{i}$ values are given where the heat generated was sufficient to allow these quantities to be calculated or where they could be estimated by other means. The mixing of $\mathrm{Na}^{+}$and I in aqueous solution did not produce sufficient heat to allow calculation of a $K$ value. However, extrapolation of the plot of $\log \beta_{1}$ for the $1: 1 \mathrm{Na}^{+}-\mathrm{I}$ reaction vs. the reciprocal of the solvent dielectric constant. $D$. (Figure 1) allows the estimation of $\log K$ for aqueous solution as 0.4 . The reactions of $\mathrm{Ba}^{2+}$ and $\mathrm{Pb}^{2+}$ with II in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ were quantitative and we were unable to calculate $\log \beta_{1}$ values from the calorimetric data. An estimate of the $\log \beta_{1}$ values for these reactions was made from the plot of $\log K$ vs. cation radius given in Figure 2. In this plot, a nearly constant difference is seen between the $\log \beta_{1}$ values in aqueous and $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ solvent for reaction 1 where $\mathrm{L}=1 I$. Assuming that similar differences exist in the cases of $\mathrm{Ba}^{2+}$ and $\mathrm{Pb}^{2+}$ in going from $\mathrm{H}_{2} \mathrm{O}$ to $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$, values of $\log K$ in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ for the reaction of these cations with II are estimated to be 6.0 and 6.5 , respectively.

The $\beta_{1}$ values for $\mathrm{K}^{+}$-I interactions in 70 and $80 \mathrm{wt} \%$ $\mathrm{CH}_{3} \mathrm{OH}$ and $\mathrm{Rb}^{+}-\mathrm{I}$ interaction in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ have large uncertainties associated with them. The uncertainty in $\beta_{1}$ in each case originates in the attempt to apportion the $\beta_{2}$ values between their constituent $K_{1}$ and $K_{2}$ values where $K_{2}>K_{1} .{ }^{17}$ Because of the uncertainties in the consecutive constants. no attempt was made to calculate $\Delta H_{i}$ values for the consecutive reactions.

## Discussion

Medium Effect on Stability and Stoichiometry of Benzo-15-Crown-5 Complexes. The free energy change for the electrostatic process involving a separation of charged species in a dielectric medium is inversely related to the dielectric constant. ${ }^{18}$ If the bonding between uncharged cyclic polyethers and charged cations is electrostatic in nature, as has been suggested, ${ }^{2,8}$ one might expect to see a similar dependence of the free energy change on the dielectric constant of the solvent. The plot in Figure 1 of $\log \beta_{1}$ vs. $1 / D$ is nearly linear, suggesting large electrostatic contributions as would be expected for the binding of $\mathrm{Na}^{+}$and $\mathrm{K}^{+}$to this ligand. Above 60 $\mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH} 1: 2 \mathrm{~K}^{+}$complexes are formed. $\log \beta_{1}$ data for


Figure 1. Plot of $\log \beta_{1}$ for the reaction $\mathrm{M}^{+}+\mathrm{L}=\mathrm{ML}^{+}(\mathrm{L}=$ benzo-15-crown-5) vs. the reciprocal of the dielectric constant.
these complexes are not included in Figure 1, since factors other than the dielectric constant, such as selective cation solvation, solvent structure changes, and ion pairing, may become important for these systems.
The heat produced from the interaction of $\mathrm{Na}^{+}$with I in aqueous solution was not large enough to calculate $\log \beta$ and $\Delta H$ values, although extrapolation of the data in Figure 1 indicates that $\log \beta_{1}$ is approximately the same for the $\mathrm{Na}^{+}$and $\mathrm{K}^{+}$complexes. This result is consistent with the finding ${ }^{4}$ that $\log K_{1}$ values for the reaction in aqueous solution of $\mathrm{Na}^{+}$and $\mathrm{K}^{+}$with 15 -crown- 5 are nearly the same ( 0.70 and 0.74 , respectively).

There is a marked increase in $\Delta H_{1}$ for the reaction of $\mathrm{Na}^{+}$ with I in going from 70 to $80 \% \mathrm{CH}_{3} \mathrm{OH}$. Although there is no evidence for $1: 2$ complex formation as is the case with $\mathrm{K}^{+}$in solvents with more than $60 \% \mathrm{CH}_{3} \mathrm{OH}$, this large increase in $\Delta H_{1}$ must reflect changes occurring in the structure of the solvent mixture or in the solvation properties of the cyclic polyether and cation at this solvent composition.
Medium Effect on Stabilities of 18-Crown-6 Complexes. Log $\beta_{1}$ values for the reaction of II with uni- and bivalent cations in aqueous solution have been published. ${ }^{4}$ The results in Table I allow comparisons to be made between $\log \beta_{1}$ values valid in aqueous and $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ solvents. The $\log \beta_{1}$ values are plotted in Figure 2, where it is seen that the curves generally are parallel, but shifted approximately $2.0 \log \beta_{1}$ units higher in the methanol solvent. The positions of maximum stability for each charge type remain approximately the same. As the methanol fraction of the solvent increases. the quantity of heat liberated per mole and the $\log \beta_{1}$ values (Figure 1) both increase for $\mathrm{Na}^{+}$. The interaction of $\mathrm{K}^{+}$with I shows similar behavior with the exceptions that sufficient heat is generated in aqueous solution to estimate a $\log \beta_{1}$ value, and 1:2 complexes are formed between $\mathrm{K}^{+}$and I in 70 and $80 \% \mathrm{CH}_{3} \mathrm{OH}$ solvents. The selectivity of benzo-15-crown-5 for $\mathrm{K}^{+}$over $\mathrm{Na}^{+}$ increases as wt $\% \mathrm{CH}_{3} \mathrm{OH}$ increases in these $\mathrm{CH}_{3} \mathrm{OH}-\mathrm{H}_{2} \mathrm{O}$ solvents. Similar results are reported by Lehn and Sauvage ${ }^{19}$ for the case of $\mathrm{Na}^{+}$and $\mathrm{K}^{+}$interaction with several cryptates, selectivity by these ligands for $\mathrm{K}^{+}$being greater in $95 \%$ $\mathrm{CH}_{3} \mathrm{OH}$ than in water. The structure of the $1: 2$ complex formed between $\mathrm{K}^{+}$and I in 70 and $80 \% \mathrm{CH}_{3} \mathrm{OH}$ is not known. However, it is likely that a "sandwich" type arrangement exists with the $\mathrm{K}^{+}$located between the two ligands as has been observed for the $1: 2$ potassium iodide-benzo- 15 -crown- 5 crystal. ${ }^{20}$ The calorimetric data for the reaction of $\mathrm{K}^{+}$with cyclic polyethers having larger ring sizes, II, III, and IV, show only


Figure 2. Plot of $\log \beta_{1}$ for the reaction $\mathrm{M}^{n+}+\mathrm{L}=\mathrm{ML}^{n+}\left(\mathrm{M}^{+} \ldots, \mathrm{M}^{2+}\right.$ -, $\mathrm{L}=18$-crown-6) in aqueous and $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ solvents. An asterisk denotes an estimated value, see text.

1:1 complexes, suggesting that in these ligands, the $\mathrm{K}^{+}$is positioned in the polyether cavity. It is not apparent why a $1: 2$ complex does not form in the case of the $\mathrm{Cs}^{+}$-I interaction in the $70 \%$ methanol solvent. However, since the experimental data were adequately fit by reaction 1 alone, the contribution from reaction 2 is assumed to be small in this case.

Comparison of $\Delta H_{1}$ and $\Delta S_{1}$ values for univalent ( $\mathrm{Na}^{+}, \mathrm{K}^{+}$, $\left.\mathrm{Rb}^{+}, \mathrm{Cs}^{+}\right)$and bivalent $\left(\mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}, \mathrm{Pb}^{2+}\right)$ cation interaction with II in aqueous ${ }^{4,21}$ and $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ solvents shows that, with the exceptions of $\mathrm{Rb}^{+}$and $\mathrm{Cs}^{+}$, the increase in $\log \beta_{1}$ is almost entirely due to an increasingly favorable $\Delta H_{1}$ change, the change in $\Delta S_{1}$ going from aqueous to $70 \% \mathrm{CH}_{3} \mathrm{OH}$ solvent composition remaining essentially constant. In the cases of $\mathrm{Rb}^{+}$ and $\mathrm{Cs}^{+},-\Delta S_{1}$ changes of 10 and $6 \mathrm{cal} /(\operatorname{deg~mol})$, respectively, are seen compared to $0,1.2,2.1,2.1$, and 3.1 for $\mathrm{Na}^{+}$. $\mathrm{K}^{+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}$, and $\mathrm{Pb}^{2+}$, respectively. Values of $\Delta S_{\mathrm{l}}$ for the $70 \% \mathrm{CH}_{3} \mathrm{OH}$ solvent were more negative than those in the aqueous solvent in all cases.

Previous studies ${ }^{4,21}$ have shown that entropy changes for $1: 1$ metal complexation with 15 -crown-5 and 18 -crown-6 in aqueous solution are generally small ( $<-10 \mathrm{cal} /(\mathrm{deg} \mathrm{mol})$ ) and negative. Several factors contribute to $\Delta S$, including relative contributions of cation and ligand dehydration, and ligand conformation changes upon complexation. In the small ring compounds, ligand conformation changes are likely small and the small $\Delta S_{1}$ changes suggest that the solvation effects are also minimal. However, there should be an increase in ring flexibility with increasing free ligand ring size, resulting in more negative $\Delta S_{\text {। }}$ values upon complexation. The data in Table I are generally consistent with this expectation. For example, comparison of $\Delta S_{1}$ values valid in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ for formation of $1: 1$ complexes of $\mathrm{Na}^{+}$, shows $\Delta S_{1}$ to be nearly constant for I and II, but to be markedly more negative for the larger ring compounds III and IV. The small $\Delta S_{1}$ values in the cases of I and II suggest that the structures of these ligands are relatively rigid and do not lend themselves to significant conformational changes. This observation is consistent with the x-ray structure observed by Bush and Truter for the $\mathrm{Na}^{+}-\mathrm{I}$ complex. ${ }^{22}$ Values of $\Delta S_{\text {, for the reaction of } \mathrm{Na}^{+} \text {with II and }}$ other 18 -crown- 6 and 15 -crown- 5 ligands in aqueous solution are likewise numerically small $(<-10 \mathrm{cal} /(\operatorname{deg~mol})) .{ }^{4}$ The $\Delta S_{1}$ values for the reactions of III and IV with $\mathrm{Na}^{+}$are substantially more negative, suggesting that significant conformational changes may be important in the formation of these complexes.


Figure 3. Plot of $\log \beta_{1}$ for the reaction $M^{n+}+L=M L^{n+}$ for several cation pairs in $\mathrm{H}_{2} \mathrm{O}-\mathrm{CH}_{3} \mathrm{OH}$ solvents.

Effect of Ring Size and Solvent Composition on Complex Stability. The absence of a reaction between the alkaline earth metal ions- $\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}$, and $\mathrm{Ba}^{2+}$-and benzo-15-crown-5 in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ is interesting, since these cations react with 18 -crown-6 in this solvent and with 15 -crown- 5 in aqueous solution. ${ }^{4}$ Change in solvent composition from water to water-methanol mixtures results in different cation selectivity patterns for 15 -crown- 5 and 18 -crown- 6 ligands. These differences are seen in part in Figures 1 and 2 and are further illustrated in Figure 3, where $\log \beta_{1}$ values for 1:1 reactions of several pairs of cations with 18 -crown- 6 and benzo- 15 -crown- 5 ( 15 -crown-5 in the case of $\mathrm{Sr}^{2+}$, Figure 3b) are compared. There is a regular increase for either the $\mathrm{Na}^{+}, \mathrm{K}^{+}$or $\mathrm{Na}^{+}, \mathrm{Sr}^{2+}$ pair in the case of 18 -crown- 6 , but for benzo- 15 -crown- 5 differentiation between either $\mathrm{K}^{+}$and $\mathrm{Na}^{+}$or $\mathrm{Sr}^{2+}$ and $\mathrm{Na}^{+}$is enhanced in the $\mathrm{CH}_{3} \mathrm{OH}$ solvent. This is especially true of the $\mathrm{Na}^{+} / \mathrm{Sr}^{2+}$ case where selectivity of $\mathrm{Na}^{+}$over $\mathrm{Sr}^{2+}$ (or other alkaline earth cations) is markedly enhanced by increasing the fraction of the $\mathrm{CH}_{3} \mathrm{OH}$ component of the solvent.

Pedersen ${ }^{2 b}$ observed that a complex is more stable (higher $\log \beta$ value) the greater the number of potential coordination sites in the ring, provided the sites are coplanar and symmetrically distributed. The two ligands in the present study which fit these requirements are I and II, ligand III (and presumably IV as well) being cylindrically symmetrical according to Pedersen. The $\log \beta_{1}$ values for I and II (Table I) confirm Pedersen's statement.

Examination of the $\Delta H_{1}$ data for the reaction of $\mathrm{Na}^{+}, \mathrm{K}^{+}$, and $\mathrm{Cs}^{+}$with I and II in $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ show $-\Delta H_{1}$ to become more positive in the case of each cation with an increase of one donor atom in the polyether ring as would be expected if the magnitude of $\Delta H_{1}$ is related to the number of metaldonor atom bonds. The larger ring compounds do not show a corresponding increase in $\Delta H_{1}$ with ring size except in the case of $\mathrm{Na}^{+}$. The $\Delta H_{1}$ and $\Delta S_{1}$ data in Table I taken together.
however, show interesting and consistent changes as a function of ligand cavity size ( 15 -crown- 5 through 27 -crown- 9 ) for the alkali metal ions. Between $\mathrm{H}_{2} \mathrm{O}$ and $70 \mathrm{wt} \% \mathrm{CH}_{3} \mathrm{OH}$ there is a large change in $\Delta H_{1}(-3.82$ to -11.74$)$ and in $\Delta S_{1}(-3.7$ to -32.5 ) for the case of $\mathrm{Na}^{+}$, which is consistent with the change which might be expected from an increase in cavity size with a consequent increase in the number of donor atoms and in ligand flexibility. This observation is interesting in connection with x -ray crystallographic data for the $\mathrm{K}^{+}$-dibenzo30 -crown-10 complex, where extensive ligand conformation change between the complexed and uncomplexed ligand is found. ${ }^{22}$ Of the two cations, $\mathrm{Na}^{+}$has the greater charge density and the $\Delta H_{1}$ and $\Delta S_{1}$ values in Table I suggest that it may be more effective than $\mathrm{K}^{+}$in ordering the large cyclic polyether ring. With the 27 -crown 9 ring, the largest negative $\Delta H_{1}$ and $\Delta S_{1}$ values are found with $\mathrm{Na}^{+}$, the latter quantity indicating that a greater ligand conformation change is required to accommodate the smaller alkali metal ion. The favorable $\Delta H_{1}$ value, however, is more than balanced in the case of $\mathrm{Na}^{+}$by the large negative $\Delta S_{1}$ value resulting in a smaller $\log \beta_{1}$ value (1.50) than that (2.76) found for formation of the $\mathrm{K}^{+}-18$ -crown- 6 complex. The need for large conformational changes to accommodate the cation with correspondingly large negative $\Delta S_{1}$ changes in the case of the more electronegative $\mathrm{Na}{ }^{+}$could account for the large selectivity of $\mathrm{K}^{+}$over $\mathrm{Na}^{+}$by macrocyclic compounds of large ring size such as valinomycin and nonactin. ${ }^{8}$ For example, the difference in the $\log K$ values for the interaction in $\mathrm{CH}_{3} \mathrm{OH}$ of $\mathrm{K}^{+}$and $\mathrm{Na}^{+}$with valinomycin is 4.3, while the corresponding difference in the $\log K$ values for the reaction of these cations with the relatively inflexible di-benzo- 18 -crown- 6 is $0.3^{23}$

## References and Notes

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